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# Analysis of Human Vergence Dynamics

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Disparity vergence is commonly viewed as being controlled by at least two mechanisms, an open-loop vergence-specific burst mechanism analogous to the ballistic drive of saccades, and a closed-loop feedback mechanism controlled by the disparity error. We show that human vergence dynamics for disparity jumps of a large textured field have a typical time course consistent with predominant control by the open-loop vergence-specific burst mechanism, although various subgroups of the population show radically different vergence behaviors. Some individuals show markedly slow divergence responses, others slow convergence responses, others slow responses in both vergence directions, implying that the two vergence directions have separate control mechanisms. The faster time courses usually had time-symmetric velocity waveforms implying open-loop burst control, while the slow response usually had time-asymmetric velocity waveforms implying closed-loop feedback control. A further type of behavior in a distinct subpopulation is a compound anomalous divergence response consisting of an initial convergence movement followed by a large corrective divergence movement with time courses implying closed-loop feedback control. The closed-loop response for slow responses to disparity steps exhibited pronounced oscillations in the velocity trace, implying the involvement of a sampled-data system with a rate of about 3 samples/s. This analysis of the variety of human vergence responses thus contributes substantially to the understanding of the oculomotor control mechanisms underlying the generation of vergence movements.

Keywords: oculomotor dynamics vergence binocular eye movements convergence divergence anomaly

## Introduction

### Vergence control

The present study focuses on the issue of binocular vergence movements and the analysis of their control mechanisms when driven by large-field changes in disparity. Disparity vergence is commonly viewed as being controlled by at least two mechanisms, an open-loop vergence-specific burst mechanism analogous to the ballistic drive of saccades, and a closed-loop feedback mechanism controlled by the disparity error (Krishnan & Stark, 1977; Semmlow et al., 1986, 1993; Hung, et al., 1986; Erkelens, 2011). The time course of the vergence-specific burst is an order of magnitude slower than the saccadic time course for the same amplitude of motion of each eye.

The existence of a burst component of disparity vergence movements, though initially contentious (Robinson, 1971; Krishnan & Stark, 1977), was established by studies such as that Gamlin & Mays (1992) and Mays et al. (1986), which showed that the change in eye position (eye velocity) was directly proportional to the firing rate of the motoneurons driving the eye muscles involved (Fig. 1). Since the vergence signals underwent a sigmoid change in position, the motoneuron burst matches the roughly Gaussian or gamma-function form of the velocity trace. Thus, it is now well established that the change in mid-brain motoneuron firing rate is linearly proportional to the vergence velocity (with a gain of 1-5 spikes/s per %s across the cell population; Mays et al., 1986; Gamlin & Mays, 1992). Thus, vergence velocity may be regarded as

an effective proxy for the firing rate of the underlying motoneurons.

The presence of the closed-loop component of disparity vergence control is consistent with the idea that the vergence waveform beyond the peak velocity should approximate the form of an exponential decay function, due to the proportional reduction in the error signal as the eye approaches the target positions (Robinson, 1975; Zee, FitzGerald & Optican, 1992). There are many cases in which the data approximate such an exponential decay. (Here we use the term “exponential” in the qualitative sense of a continuously decreasing velocity as the eyes asymptote to the final position, without attempting to assess how well it conforms to a mathematical exponential of the form  $e^{-x}$ ).

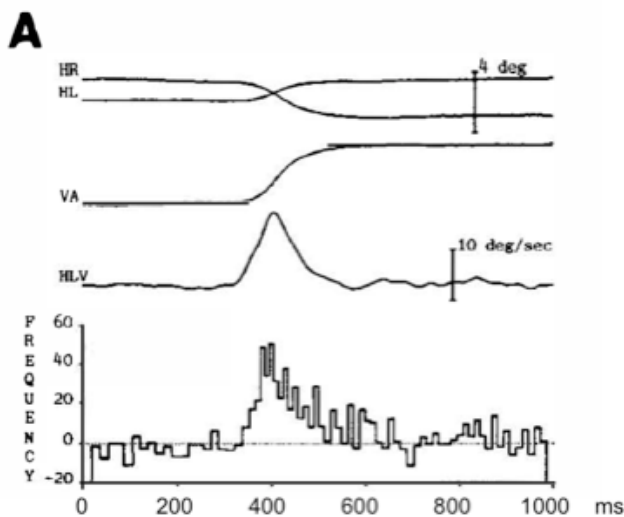


Fig. 1. Monkey vergence response reproduced from Gamlin & Mays (1992), showing the right and left horizontal eye position traces (HR, HL), the difference trace of vergence amplitude (VA), the corresponding vergence velocity trace (HLV) and the concomitant change in firing rate of a midbrain medial rectus motor neuron recorded in the oculomotor nucleus during the movement. Note the similarity between the waveform of the velocity trace and motor neuron firing burst, which both have relatively long durations of about 200 ms.

The presence of two processes feeding into the motoneurons is further implied by the ‘dual mode theory’ of Hung, Semmlow & Ciuffreda (1986) and Semmlow & Yuan (2002), based on an independent components analysis of the variations in the disparity vergence responses, implying that vergence movements consist of a rapid transient

component and a slower sustained component. However, it should be noted the assumption of independent components analysis is that the components are invariant in temporal waveform (varying only in their relative amplitudes), although it is well known that vergence movements have variability of their temporal parameters, which could give a spurious result of an initial transient component under the incorrect assumption of temporal invariance. The independent components analysis is therefore not by itself convincing evidence of a separate transient component to disparity vergence.

Recent work on the optimal control theory of saccadic dynamics suggests that the saccadic waveform is tuned to jointly minimize the duration and accuracy of each saccade (Harris & Wolpert, 1998; 2006; Tanaka, Krakauer & Qian, 2006; Xu-Wilson et al., 2009). At least for small saccades, this theory predicts a time-symmetric velocity function for the saccadic waveform, approximating a half-cosine waveform. Based on the empirical results of the dual-mode theory, we take this to be the signature of the transient component.

If valid, this ‘dual mode’ analysis implies that the open-loop component of vergence movements would have the same waveform structure as a saccade, although far slower in time course. This concept suggests that the waveform of open-loop component should be time-symmetrical (in the sense that the waveform velocity, or temporal derivative of the waveform, has symmetrical rise and fall times). This symmetric form is driven by a (slow) burst of activity in the oculomotor neurons driving the vergence movement and is formally distinguishable from the exponential concept of the closed-loop component, which implies a time-asymmetrical waveform as the feedback progressively reduces the error to zero. We will use this difference in time-symmetry of the two components as a key to their relative predominance in our subject populations.

## Types of vergence dynamics

In terms of peak velocity, it is well established that there is a ‘main sequence’ function of peak velocity vs. amplitude for disparity vergence eye movements, very similar to that for saccades (Rashbass & Westheimer, 1961; Hung et al., 1994; Erkelens et al., 1989). The summary data of the latter study show a roughly linear increase in vergence velocity with amplitude up to about  $2^\circ$ , with a progressive saturation of the curve for larger amplitudes. For reference, the slope of the linear portion is about  $7^\circ/\text{s}$ .

It is also well known that disparity vergence is not always perfectly matched between the two eyes, i.e., with

matching time-functions in opposite directions in the two eyes (Collewijn, Erkelens & Steinman, 1995). Instead there is often reported to be an asymmetrical saccade in one eye (even when the target motion is perfectly symmetrical), which may be seen as the vergence system employing a biased strategy to achieve a faster acquisition of the vergence target (Coubard & Kapoula, 2008).

The third well-known disparity vergence behavior is seen for the situation of asymmetrical vergence to a laterally off-center target, in which case a uniocular saccade is typically used to bring the eyes to the average position required by the target endpoint, with a slow convergence movement (which should have the exponential waveform) to complete the motion (Collewijn, Erkelens & Steinman, 1995). In particular, Horng et al. (1998) reported that the initial open-loop component of disparity vergence could be much reduced or absent in the divergence direction, although this conclusion was based on recordings from only two subjects, and other studies have not reported such a convergence/divergence imbalance.

Two kinds of disparity vergence movement are excluded from this account. One is the case of symmetrical vergence saccades with the normal saccadic time course but in opposite directions in the two eyes. This form of saccadic eye movement is considered to be specifically prohibited in the conventional account, although the explicit mechanism of the prohibition is obscure.

## Vergence latencies

This account of the vergence dynamics would be incomplete without a consideration of the vergence latencies, which are generally included as a free parameter in the cited models of vergence control. It is noteworthy that the vergence latencies are quite similar to those of saccades, at around 200 ms. Any differences reported in the literature are likely to be attributable to sampling differences between the subject groups and the details of the method used to specify the time of onset of the respective movements. On this view, the latency for the initiation of both saccades and vergences is attributable to cortical processing of the sensory stimulation providing the impetus for the eye movements, i.e., the computational processes specifying the required amplitude and direction of the movements and the decision to initiate the movements (since they are essentially voluntary in character and can be suppressed if necessary). Once initiated, the control for the activation is passed to the oculomotor control systems of the brainstem and cerebellum, which evidently treat the two kinds of oculomotor requests very differently, but it is

likely that the cortical processing is basically similar in the two cases.

## Rationale

Based on the foregoing overview, the main goal of the present paper is to reassess the status of symmetrical vergence movements and the extent to which they are achieved either by the open-loop (burst) or the closed-loop (exponential) component of the neural control system. This reassessment will be achieved by evaluation of the temporal asymmetry of the vergence velocity profiles around the peak velocity for a large number of subjects. The exponential decay form of the closed-loop model would have a highly asymmetric profile, while the open-loop burst model should be close to symmetric (similar to that for typical saccades; Harris & Wolpert, 1998). The temporal asymmetry criterion is thus a good indicator of the underlying mechanism of vergence control, and is quantified in the form of a temporal asymmetry index (see Methods).

A further goal of the paper is to evaluate the form of the vergence dynamics to full-field targets. In the world, when an object moves toward or away from the eyes, or when we move through the world, large regions of texture typically stimulate the retina. However, many oculomotor studies use only small targets to stimulate the vergence system. Here we evaluate the disparity vergence component of such large field stimulation, showing that anomalous forms of vergence eye movements are in fact encountered at an unexpectedly high frequency.

## Methods

### Recruitment

This study involved a recruited base of 68 participants (59% female) from a non-academic population via a social media website for the normative study of oculomotor dynamics, passing the exclusion criterion of having no clinical history of brain or ocular abnormalities, including traumatic brain injury events. All recruitment and experimental procedures in this study adhered to the Declaration of Helsinki.

The participants met the criteria of letter acuity of 20/40 or better in both eyes (Bailey-Lovie chart, mean LE denominator –  $23 \pm 5$ , mean RE denominator –  $24 \pm 6$ ), and of passing a random-dot stereopsis test at a disparity of 4 arcmin. The ages ranged from 19 – 60 (mean –  $36 \pm 12$ ).

## Oculomotor procedures

Binocular eye movements were recorded with the Visagraph III binocular infrared limbal eye tracker, which has a sampling rate of 60 Hz and a typical noise level of  $\sim 4$  arcmin standard deviation in each eye for live human recordings (as assessed from the variability during fixation periods in the most stable participants). This assessment provides a net vergence noise level of  $\sim 3$  arcmin after the four-point elliptical (third-order) smoothing applied to the eye movement traces. Of course, the measured variability would also take into account the physiological variation in the fixation capability and oculomotor stability of each participant, so would typically be much larger than the irreducible measurement error, but we note that many participants achieved calibrated mean standard errors of the repeated vergence signals close to the estimated optimal level of about 3 arcmin (see Figs. 3-11).

## Horizontal position calibration series

To calibrate the linearity of the recorded position function, a  $0.4^\circ$  cross-hair monocular fixation target underwent two randomized sets of horizontal position shifts over the range from  $-16$  to  $16^\circ$  for each eye, with button presses indicating when fixation was accurate at each position. The full set of points was fitted with a third-order polynomial to provide a linear calibration of the horizontal position separately for each eye.

## Rapid horizontal disparity vergence jumps

Binocular eye movements are recorded while the  $30 \times 30^\circ$  noise field incorporating a  $1^\circ$  central fixation target underwent  $2^\circ$  horizontal square-wave disparity changes every 2-3 s, with random jitter over 1 s from a uniform distribution to avoid predictability of the onset time. The minimum interval of 2 s allows comfortable completion of repeated normal vergence movements.

## Oculomotor time series analysis

The vergence (left-eye minus right-eye) signal waveform were extracted from a period around the times of the instantaneous transitions of the stimulus in a window from 1 second prior to the transition to 2.5 seconds after the transition. The sets of converging eye movement transitions were analyzed separately from diverging eye movements. Each event response was re-zeroed by removing the mean value over the 100 ms preceding the transition. Non-representative individual responses were excluded from the analysis by iteratively removing responses whose mean squared error over time from the mean across non-excluded responses was beyond 2 standard deviations of

the mean error. (In no case were more than 3 responses excluded under this procedure.)

The average non-excluded vergence signal was numerically differentiated to derive the vergence velocity signal for each direction of eye movement for each subject. To account for noise and drift, the full duration of the vergence movements was defined as the time from the last crossing of 5% of the peak velocity prior to the time of the peak to the first crossing of 10% of the peak velocity after the peak. (The limits are asymmetric because the onset variance was smaller than the offset variance as a consequence of the respective distances from the zeroing region.) The portions of the velocity traces beyond these limits are blocked out to focus the presentation on the degree of symmetry **during** the primary vergence movements.

## Temporal Asymmetry

Temporal asymmetry of the velocity trace was defined by computing the ratio of the post-peak area minus the pre-peak area to the total area of the vergence interval defined from the velocity trace. In principle, this temporal asymmetry index has a value of 0 for a time-symmetric waveform and a value of 1 for a pure exponential waveform. In practice, the smoothing applied to the waveform reduces the maximum value for the pure exponential response after the filtering of the waveforms, so we defined a **Normalized Temporal Asymmetry Index ( $\gamma$ )** as the ratio of the empirical temporal asymmetry index to the theoretical temporal asymmetry index for a filtered exponential decay. (Note that a waveform with an asymmetry sharper than the exponential form could have  $\gamma > 1.0$ ).

## Statistical Analysis

The statistical analyses were performed by t tests. Unless otherwise noted, significant results are reported at level of  $p < 0.01$ . Results reported as non-significant did not pass the criterion of  $p < 0.05$ .

## Group Categorization Analysis

The disparity vergence dynamics estimates were not homogeneous across the population, but had a surprising variety of response characteristics. In order to formalize the categorization process, we took the approach of finding approximately Gaussian groupings of the participants according to the duration parameter of the vergence responses. The first step was to restrict the analysis to the population of well-formed responses by weeding out all unreliable responses and those that did not achieve an amplitude criterion of a least half the disparity demand of  $2.0^\circ$  within an onset latency of 500 ms. Fifty-four individuals (77%) met these criteria for well-formed responses.

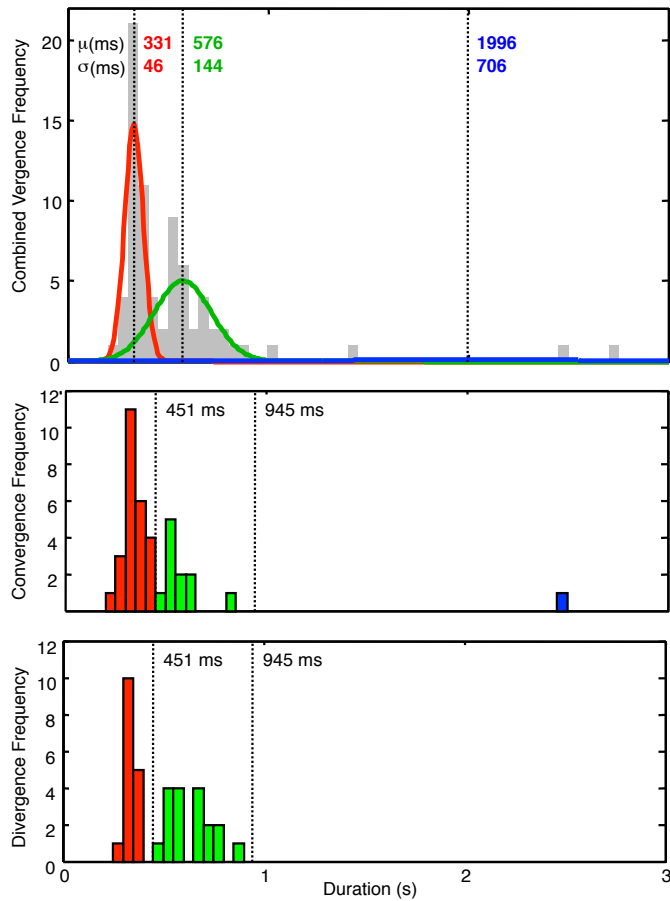


Fig. 2. Top panel: Gaussian Mixture Model cluster analysis of all well-formed vergence response durations, showing the fit for the optimal 3-Gaussian case (red, green and blue curves), with respective mean  $\pm \sigma$  parameters. Center panel: Distribution of convergence duration clusters with cluster boundaries at 451 and 945 ms. Bottom panel: Distribution of divergence duration clusters, similarly.

The next step was to group all the vergence durations (convergence or divergence) into a single group and apply a Gaussian mixture cluster routine to determine the optimal number of Gaussian clusters to categorize the durations. The optimization error was specified according to the Bayesian Information Criterion (Schwartz, 1978) over fits from 1 to 12 Gaussians, which reached a minimum with three-Gaussian model. The three Gaussians best fitting the distribution are shown in Fig. 2. (Note that the blue curve for the long-duration fit is close to the duration axis.) The cluster boundaries between adjacent distributions were determined from the upper 1% cutoffs of each Gaussian, which occurred at 451 and 945 ms, defining three duration ranges: typical, mid and slow vergence durations (T, M and S, respectively). These boundaries were then applied separately to the convergence and divergence duration distributions, respectively, to form nine dual-criterion categories in principle.

A final category (ACD) that will be specified in detail in Results had divergence responses that did not pass the initial screen because they began by consistently converging prior to initiating the divergence movement (Anomalous Compound Divergence). This behavior implied that the divergence latency failed the screening criterion of  $< 500$  ms, although the divergence velocities once initiated were within or close to the typical range of  $\sim 10^\circ/\text{s}$ .

## Results

### Disparity vergence dynamics

Before analyzing the results in detail, the quantitative indices of median latency, duration, peak velocity and temporal asymmetry, together with their  $\pm$  standard errors of the means (SEM) are presented in tabular form in Table I. The proportion of subjects falling into each category is tabulated in the first row of the table.

Table I: Vergence Dynamics Parameters for the Vergence Groupings

	TYPICAL CONV (ALL)		TYPICAL DIV (ALL)		TYPICAL BOTH		TYPICAL CONV (ONLY)		TYPICAL DIV (ONLY)		MID BOTH		MID CONV (ONLY)		MID DIV (ONLY)		SLOW VERGENCE		ACD (DIV)		ACD (CONV)	
N (%)	62		32		22		28		10		12		10		22		6		18		(18)	
Convergence	Median	SEM			Median	SEM	Median	SEM	Median	SEM	Median	SEM	Median	SEM	Median	SEM	Median	SEM	Median	SEM		
Median latency (ms)	252	27			252	37	275	40			198	25	144	52			300	33	233	14		
Peak Velocity (deg/s)	9.5	1.5			10.3	2.8	8.1	1.4			7.3	1.6	6.0	1.1			8.1	1.1	10.2	1.2		
Duration (ms)	333	12			330	18	341	17			538	25	585	17			316	47	317	33		
Templ Asymm	0.17	0.18			0.09	0.06	0.16	0.32			0.27	0.11	0.64	0.26			-0.77	0.12	-0.84	0.15		
Divergence																						
Median latency (ms)			283	32	317	35			283	32	200	54			211	43	266	95	650	110	133	18
Peak Velocity (deg/s)			-9.6	1.5	-9.1	1.9			-7.9	1.5	-5.0	1.3			-5.9	4.4	-3.8	0.2	-10.3	2.9	5.5	1.0
Duration (ms)			337	10	317	12			317	10	700	25			567	23	1433	516	554	59	483	45
Templ Asymm			0.16	0.05	-0.06	0.06			0.16	0.05	0.01	0.57			-0.20	0.16	0.67	0.24	1.07	0.18	-0.91	0.22



## Typical convergence/divergence responses

The ‘typical’ response group is defined as those individuals with vergence movements in the short-duration range, up to about 450 ms in duration, for both the convergence and divergence directions. Examples of convergence movements for six individuals from the typical convergence/divergence group are shown in Fig. 3. For convergence responses in this typical group, the median latency

was  $252 \pm 37$  ms, a typical peak velocity of  $10.3 \pm 2.8$  °/s, and median total duration of  $330 \pm 18$  ms, none of which are significantly different from the values for the larger group of typical convergence responses. Also, the velocity values are not significantly different from the corresponding velocity on the vergence main sequence summarized by Hung et al. (1994).

## Convergence

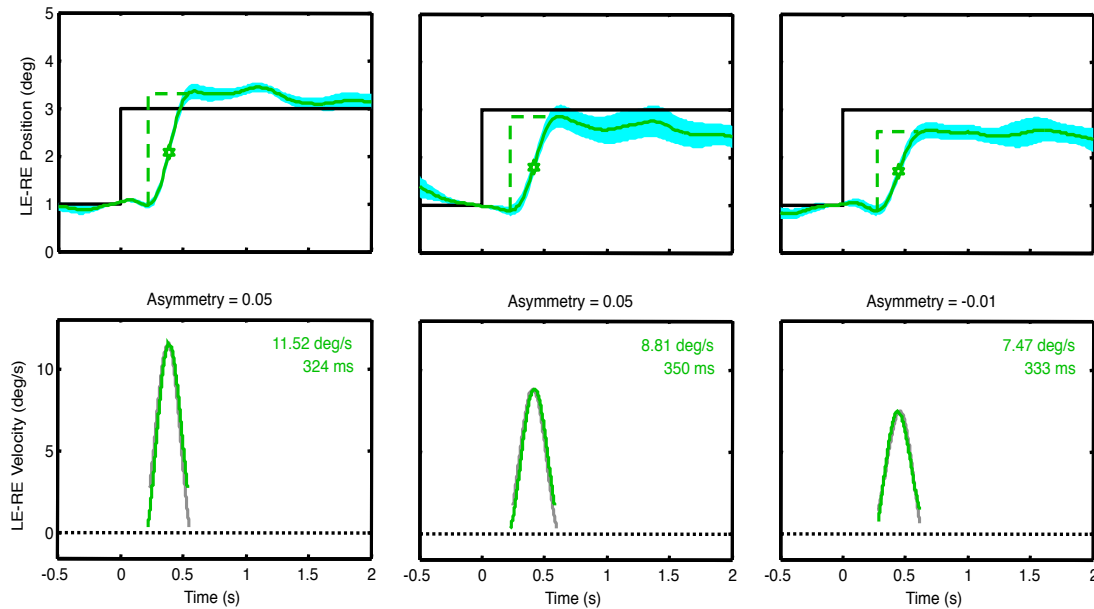


Fig. 3. Upper plots: Examples of typical mean convergence responses for three individuals (green curves, each averaged over 10-12 responses). Black line indicates the stimulus disparity change event. Gray dotted lines show the estimated amplitude and duration of each vergence movements. Cyan region represents the  $\pm 1$  SEM range of the variability over the 10-12 repeats for each trace. The star marks the point of peak velocity. Lower plots: Corresponding velocity profiles for the same average responses (color curve), together with the time-inverted velocity profile (light gray curve) aligned with the peak of each response to illustrate its degree of temporal asymmetry, quantified above each velocity panel. Note the high degree of symmetry (near-zero asymmetry) of these typical examples. Duration and peak velocity values are estimated from the velocity trace as described in Methods.

## Typical divergence responses

In the group of individuals with typical response dynamics for both convergence and divergence movements, typical divergence responses had the following characteristics: latency of  $317 \pm 37$  ms, typical peak velocity of  $-9.1 \pm 1.9$  °/s, and a total duration of  $317 \pm 12$  ms. Examples are shown in Fig. 4. These values indicate that none of the

dynamic parameters for the typical divergence response are significantly different from those for the convergence movements. These parameters are again different by an order of magnitude from those of typical saccades (see Fig. 4), indicating that the participants did not typically resort to saccadic strategies to achieve the divergence targets.

# Divergence

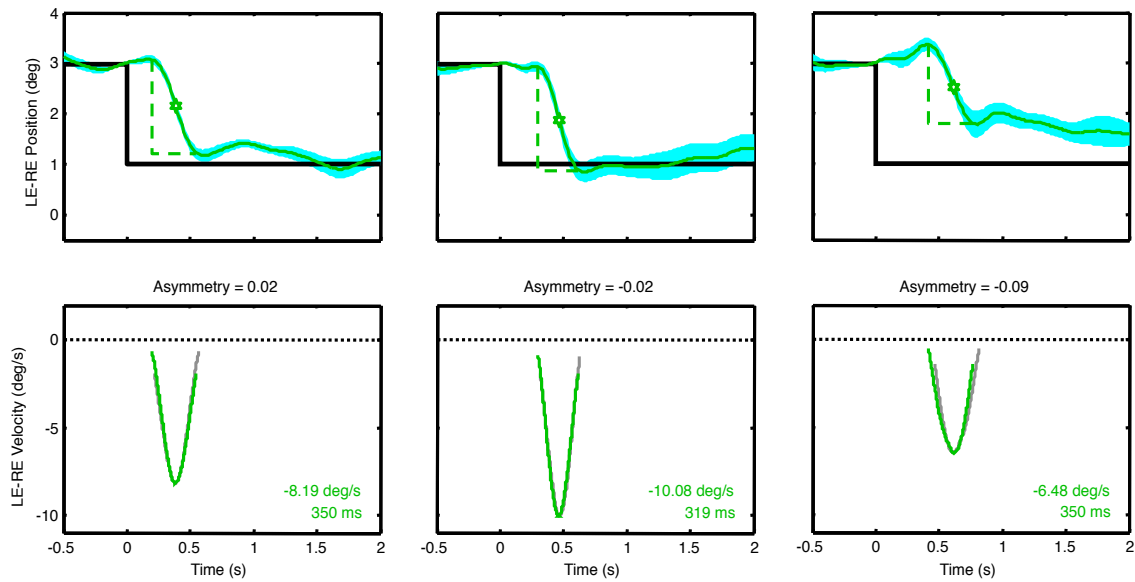


Fig. 4. Examples of typical mean divergence responses and velocity traces for the same sample of typical subjects and plotted with the same conventions as Fig. 3. Note the high degree of symmetry (near-zero asymmetry) of these typical examples of divergence.

## Temporal Asymmetry

Across the group of typical subjects, the Normalized Temporal Asymmetry Index for the group (62%) of typical convergence response rates had the value of  $\gamma = 0.17 \pm 0.18$ , not significantly greater than zero. Because this superordinate grouping has some heterogeneity, we may

evaluate the asymmetry for the smaller group with typical responses in both directions, for which the asymmetry had the tighter range of  $\gamma = 0.09 \pm 0.06$ , again not significantly different from zero. We may conclude that, for this wide-field texture stimulus at the disparity convergence amplitude of  $2^\circ$ , there is no significant positive temporal asymmetry in the convergence response.

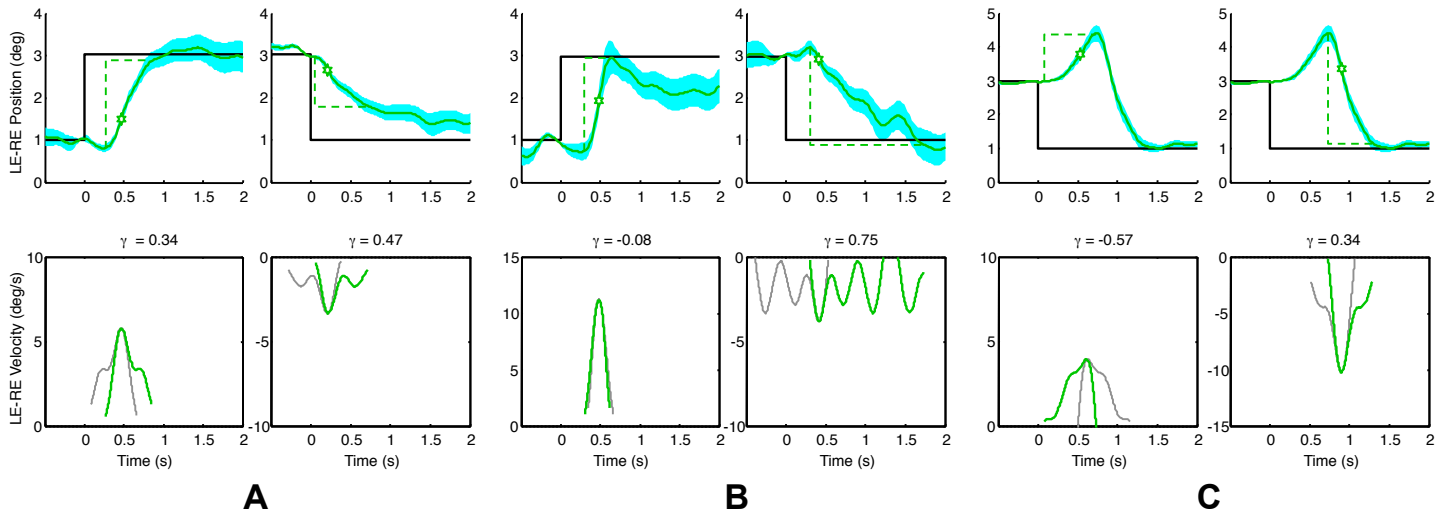


Fig. 5. Examples of typical mean vergence responses and velocity traces for responses showing temporal asymmetries, plotted with the same conventions as Fig. 3. A: Convergence/divergence example from the Mid Both category. B: Convergence/divergence example from the Slow Divergence Only category. C: Divergence example from the Anomalous Compound Divergence category, analyzing the **same divergence response** for asymmetry separately in the two vergence directions.



The Normalized Temporal Asymmetry Index was similar for the divergence responses of the superordinate group with typical divergence response rates. The net asymmetry was again small, at  $\gamma = 0.16 \pm 0.05$ , though significantly positive in this group. For the smaller group with typical responses in both vergence directions, the divergence asymmetry was, however, not significantly different from zero,  $\gamma = -0.06 \pm 0.06$ . Thus it seems that, in the fully typical individuals of the Typical Both group, divergence responses do not inherently have a different temporal form from convergence responses (Horng et al., 1998), although convergence/divergence differences will become apparent as the less typical groupings are analyzed.

To introduce the properties of the temporal asymmetry, we have to anticipate somewhat the grouping results, so refer to the relevant sections for full details of those responses. The first case (Fig. 5A) is an example of strong asymmetry for both convergence and divergence, from the Mid Both vergence response category (see Table I). The range of the analysis is described in Methods. Note the separation between the forward time (green curves)

and reverse time (gray curves) plots of the velocity plots, defining the waveform asymmetry. The second case (Fig. 5B) is from the group of slow divergence responses with typical convergence responses. Note the tight overlap of the convergence velocity traces in contrast to the strong temporal asymmetry of the divergence traces. The pronounced oscillations of the slow velocity signals are typical of the slow response group, and are considered in detail below. The third quartet of panels (Fig. 5C) is a typical case from the Anomalous Compound Divergence group, in which the divergence response is reliably preceded by an inappropriate convergence movement. Rather than analyzing the responses to the convergence and divergence stimuli (as in the previous panels), here we analyze the convergence and divergence **components** of the compound divergence movements. While the divergence component has a positive temporal asymmetry similar to the other cases, the convergence component shows a strongly **negative** value of temporal asymmetry, implying a more gradual onset than offset time-course. The interpretation of these asymmetry features is left to the discussion.

## Typical Saccades

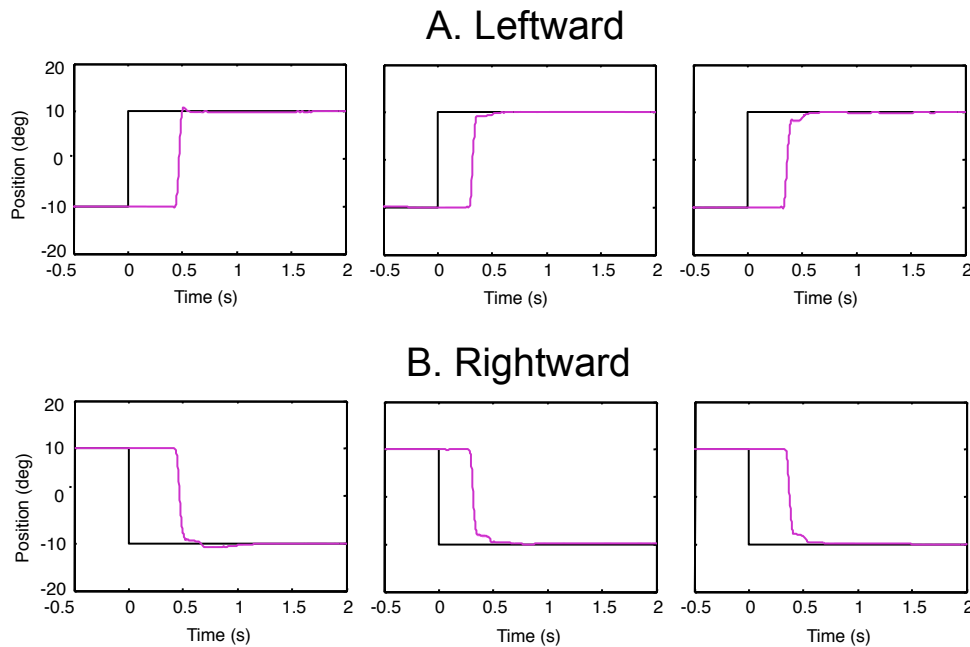


Fig. 6. Average position and velocity traces for leftward (upper panels) and rightward (lower panels) saccades averaged over 12 repeats for the subjects of Figs. 3 and 4, showing the similar latencies and much faster time courses in relation to the vergence responses. The SEM as a function of time is shown as the pink shaded region around the traces. The fact that this error region is barely visible reveals the high consistency of the saccadic performance, including the corrective saccade following the main saccade in most cases.

### Vergence/saccadic interactions

Before considering the role of vergence/saccadic interactions, we include here an analysis of the saccadic responses

of the same subject group (and on the same timescale) as Fig. 3 & 4 as a basis for comparison (Fig. 6). The saccadic stimulus was a  $1.25^\circ$  circle/cross combination jumping between horizontal positions  $10^\circ$  to the left and right

of primary (straightahead) position, with a temporal delay randomized over a flat distribution between 2s and 3s. The average saccades over 12 repeats show the typical latencies, similar to those of the typical vergence group ( $316 \pm 68$  ms), and typical saccadic durations of about 80 ms (see Bahill et al., 1975a).

We note that many subjects exhibit a habitual pattern of a slight saccadic undershoot followed by a corrective saccade, with an almost invariant pattern across the 12 repeats (shown as the barely-visible pink penumbra

around the purple time courses in Fig. 6). The timing of the corrective saccade was  $173 \pm 33$  ms with a peak velocity of  $38^\circ/\text{s}$ , similar to the values found in the original studies of this phenomenon (Becker & Fuchs, 1969; Becker, 1972). This information is included to provide reassurance that the saccadic dynamics recorded under the present conditions are, as expected, very different from the vergence dynamics (about 4 times shorter duration, even though their amplitude was  $\sim 10$  times larger in each eye).

### Individual vergence step response

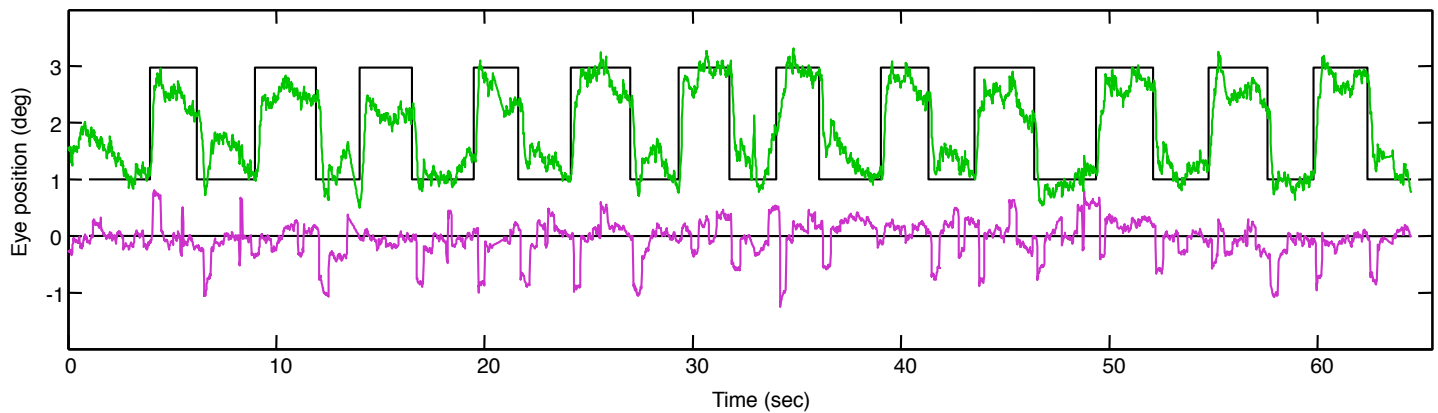


Fig. 7. Example of the saccades occurring during a vergence stimulation series of  $1\text{--}3^\circ$  vergence jumps over 12 irregular cycles (black line). The vergence signal of the difference in position between the two eyes (green curve) shows an approximate match to the stimulus disparity with a delay of a few hundred milliseconds. The mean position of the two eyes over time (magenta curve) shows general stability around the mean stimulus position (zero disparity) overlaid with microsaccades of less than  $1^\circ$  amplitude, which often occur at or after the completion of the vergence responses.

In general, saccadic activity should not be expected to be a strong component of the symmetrical vergence response. In practice, the typical case is shown in Fig. 7, where symmetrical vergence is accompanied by self-corrective microsaccades that often have a boxcar form with a saccade following the vergence movement and a correction a few hundred milliseconds later. They represent the subjects' saccadic refixations within the  $1.25^\circ$  fixation target. The saccades in Fig. 7 are conjunctive (lower trace), averaging out to a level that is undetectable relative to the prevailing noise level in the raw vergence difference waveform (upper trace). In this example, the saccades are mainly to the right for both convergence and divergence movements, but there was no consistent pattern across subjects. As can be seen in the averaged vergence responses of Figs. 3 and 4, there is no evidence of a consistent saccadic component contributing to the vergence responses; the vergence durations are of the order of 320 ms (see Table I), with no hint of a coordinated saccadic jump anywhere along the averaged vergence waveforms (Figs. 3 & 4).

### Midrate vergence responses

As indicated in Fig. 2, about 1/3 of the sample had vergence responses of up to twice the duration of the typical rate in one or both vergence directions. According to the cluster analysis, these responses formed a distinct category with median durations of  $\sim 450$  -  $\sim 950$  ms, some for convergence, some for divergence and some for both. Of those with midrate vergences in both directions (12% of the sample; see Fig. 8), the median durations were  $538 \pm 25$  ms and  $700 \pm 25$  ms for convergence and divergence, respectively, significantly longer than for the typical vergence cases. The peak velocities were significantly lower than for the typical groups, at  $7.3 \pm 1.6^\circ/\text{s}$  and  $5.0 \pm 1.3^\circ/\text{s}$ , as might be expected from the significantly longer durations. The median latencies, on the other hand, were at the low end of the typical range, at  $198 \pm 25$  ms and  $200 \pm 54$  ms, indicating that there was nothing abnormal about the initiation processes. The midrate vergence parameters for the other two groups, those with midrate vergence in one direction but not the other, were not significantly different from those of the 'both' group with two exceptions, i) that the Normalized Temporal Asymmetry Index of divergence for the Midrate Convergence group was significantly higher

than for the Mid-Rate Both group (or for the Typical group), and ii) that the divergence duration for the Midrate Divergence group was significantly shorter than for the

Mid-Rate Both group (though significantly longer than typical) (see Table I).

## Mid-rate Convergence/Divergence Responses

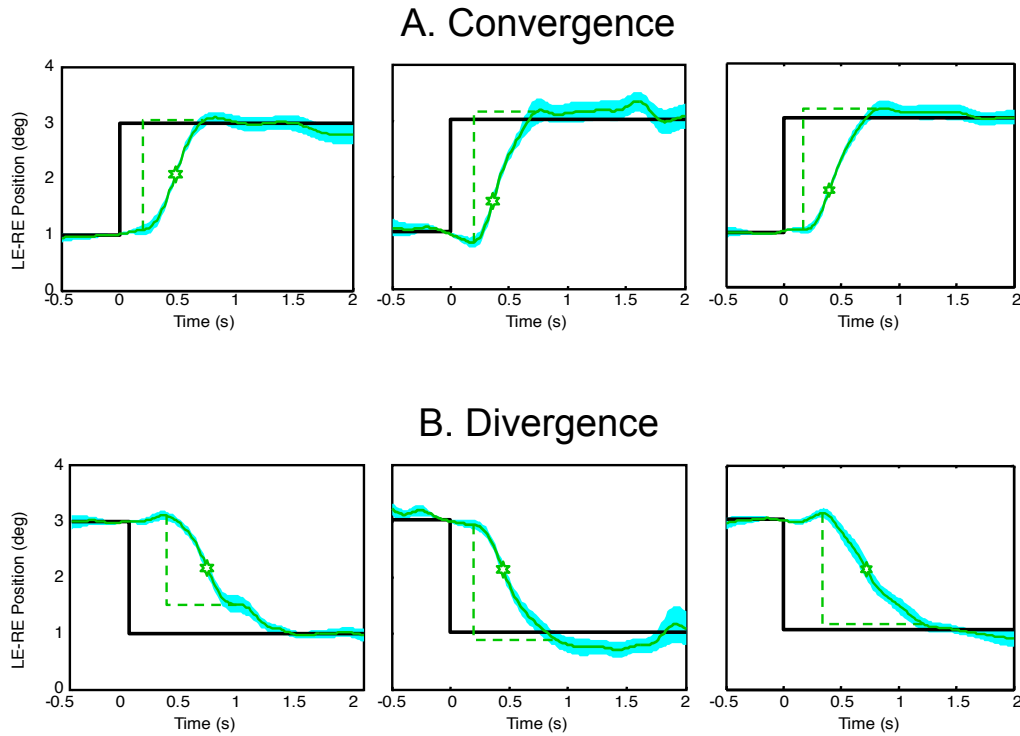


Fig. 8. Examples of typical mid-rate convergence responses and velocity traces plotted with the same conventions as Fig. 3.

### Fast convergence / slow divergence

A subgroup of four individuals of this sample of non-TBI and non-strabismic individuals had much slower vergence responses (duration > 945 ms) in either the convergence or divergence direction, although none of the sample had such slow responses in both directions. Since only one was a slow convergence case, that one does not qualify as a group, so we will only consider the group statistics for the slow divergence group (Fig. 9). The convergence responses all fell in the typical range with a median latency of  $300 \pm 33$  ms, a total duration of  $316 \pm 47$  ms, and a typical peak velocity of  $8.1 \pm 1.1$  %/s, all of which are similar to those of the typical group. The divergence re-

sponses had much slower responses of  $-3.8 \pm 0.2$  %/s with correspondingly longer durations of  $1433 \pm 516$  ms, but typical latencies of  $266 \pm 95$  ms.

The asymmetry assessment can be used to evaluate the hypothesis that the slow responses derive from a missing open-loop vergence system (see Discussion). The Normalized Temporal Asymmetry Indices for the slow vergence responses were different for the convergence and divergence directions. In the convergence direction the temporal asymmetry had the significantly negative value of  $\gamma = -0.77 \pm 0.12$ , while for the divergence direction it was significantly positive at  $\gamma = 0.67 \pm 0.24$  (significantly higher than the typical value for divergence responses).

## Fast convergence / slow divergence

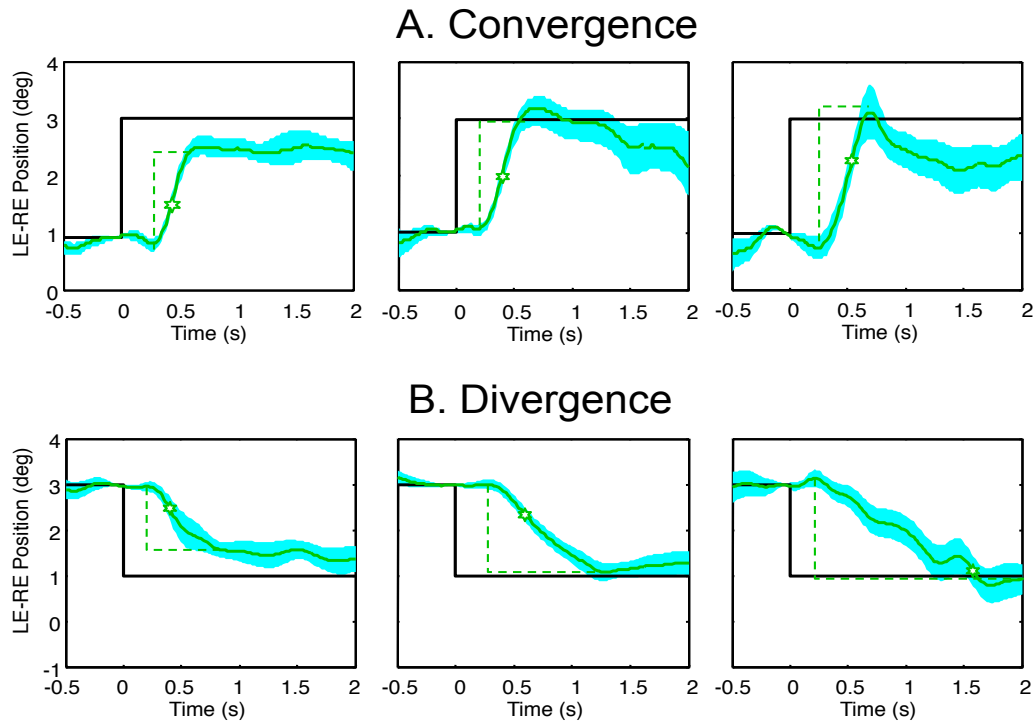


Fig. 9. Examples of vergence movements from three individuals with typical convergence responses but slow divergence movements, plotted with the same conventions as Fig. 3. The vergence movements are repeatable to within a standard error of a few arc min.

### Slow vergence oscillations

To provide further insight into the nature of the control mechanism for slow vergence movements, we selected all the responses conforming to the character of dominance by the closed-loop feedback vergence control system, defined as those with a duration longer than 1 s **and** a temporal asymmetry index  $\gamma > 0.5$ . To take a detailed look at these responses, a sample of three of them are plotted in Fig. 10, together with their velocity profiles. Although characterized earlier by the temporal asymmetry analysis

as roughly approximating exponential waveforms in the disparity position traces, the velocity plots for these slow responses all show pronounced oscillatory behavior in the vergence velocity plots (colored lines), making clear that the presence of oscillations is a reliable feature of the slow, time-asymmetric vergence responses in either the convergence or divergence directions. The average oscillation frequency for this group was  $3.02 \pm 0.12$  Hz, implying that the samples were being taken at a rate of about 3 samples/s, similar to the typical fixation rate.

## Slow (0.3 Hz) Vergence Velocity Oscillations

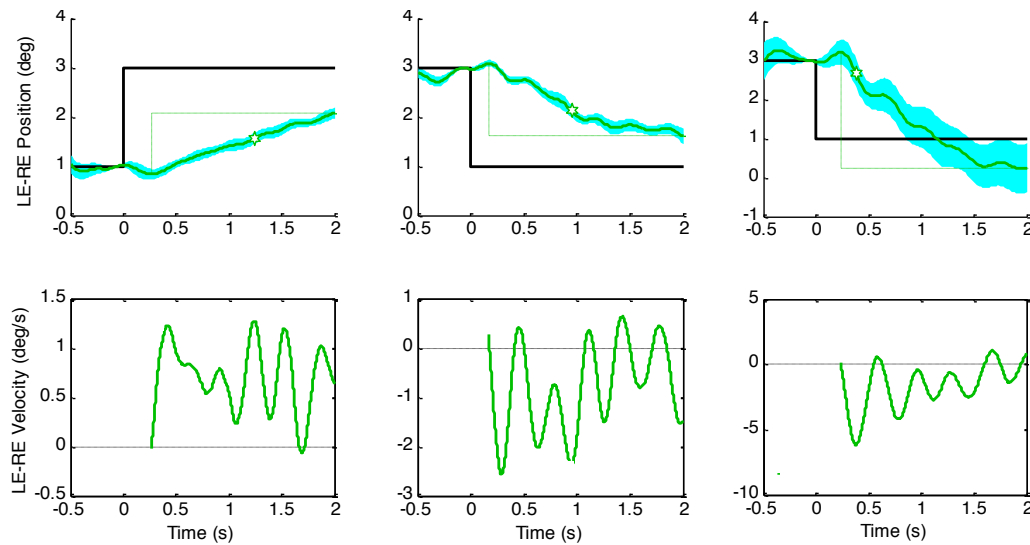


Fig. 10. Assemblage of the mean vergence amplitude (upper plots) and velocity (lower plots) waveforms for a sample of vergence responses meeting the criteria of a duration  $> 1$  and an asymmetry index  $> 0.5$ . Note pronounced oscillations in the vergence velocity plots (colored curves). Other conventions as in Fig. 3.

### Anomalous compound divergence response

A substantial subgroup of nine individuals from this study (with no strabismus or reported TBI) showed a profound inability to make prompt disparity-driven divergence movements. Instead, the divergences were preceded by an initial convergence movement before the required divergence could take place. A raw 60 s vergence record of the 12 repeats of the convergence/divergence cycles for one such subject is shown in Fig. 11. Note that, on this 60 s time scale, a saccade appears as an almost-vertical line in the trace, of which only three are visible (at 17, 36, and 52 s). The time courses of the anomalous vergence move-

ments (the 2 s spike after each divergence stimulus) were non-saccadic, with typical vergence dynamics (compare Figs. 4 & 5).

Averages of convergence and divergence responses over 12 events (see Methods) are plotted for three such subjects in Fig. 12. The upper panels show that the convergence movements were within the typical range, with average latencies of  $233 \pm 14$  ms, average durations of  $317 \pm 33$  ms, and average velocities of  $10.2 \pm 1.2$  °/s, none of which are significantly different from the typical values. The one parameter that did differ from the typical value was the temporal asymmetry of  $\gamma = -0.84 \pm 0.15$ .

### Individual Anomalous Compound Divergence Response Series

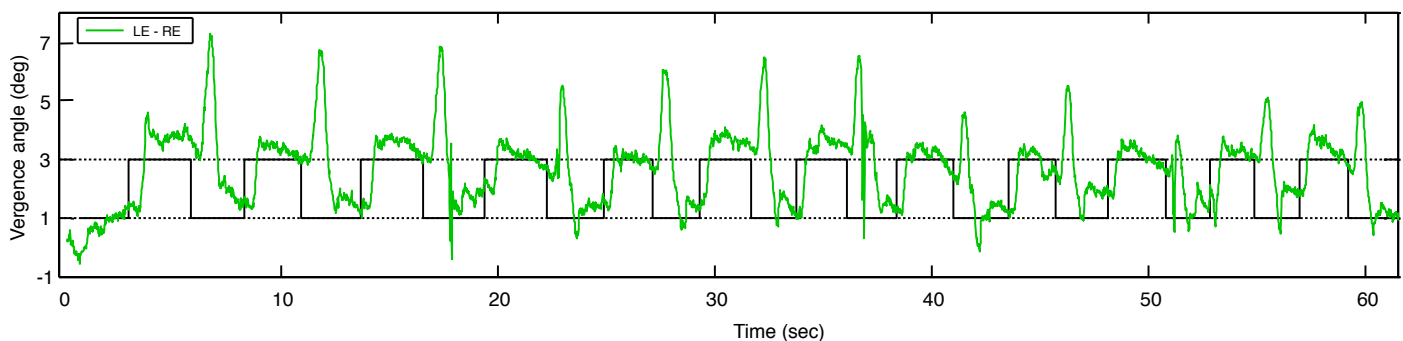


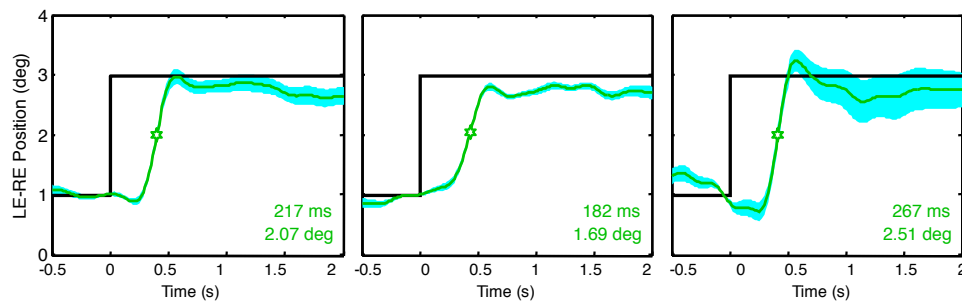
Fig. 11. An individual 60 s time series of step disparity vergence movements in one case, showing repeated anomalous compound responses to the divergent disparity stimulus, with the divergence movement preceded consistently by a full convergent movement in the opposing direction. Black trace is the stimulus disparity to be tracked. Note that none of these anomalous vergence movements had a significant contribution from differential (asymmetrical) saccades, which appear as fast spikes on this time scale. The saccades on cycles 3, 7 and 10 are all bidirectional, with little net effect on the vergence angle.

Only when this convergence movement was completed did the eyes begin a divergence movement, usually immediately but in one case after about a second's delay. In most cases, the divergence movement was longer than the normal divergence movement ( $554 \pm 59$  ms), sufficient to correct for the initial convergence to bring the eyes close to the required vergence posture at the typical

vergence velocity ( $10.3 \pm 2.9$  °/s). These divergence movements had the largest values for temporal asymmetry of any vergence movement ( $\gamma = 1.07 \pm 0.10$ ) indicating that they were on average close to the exponential form, implying that the open-loop burst mechanism for divergence was inactivated in these individuals.

## Anomalous Compound Divergence Responses

### A. Convergence



### B. Divergence

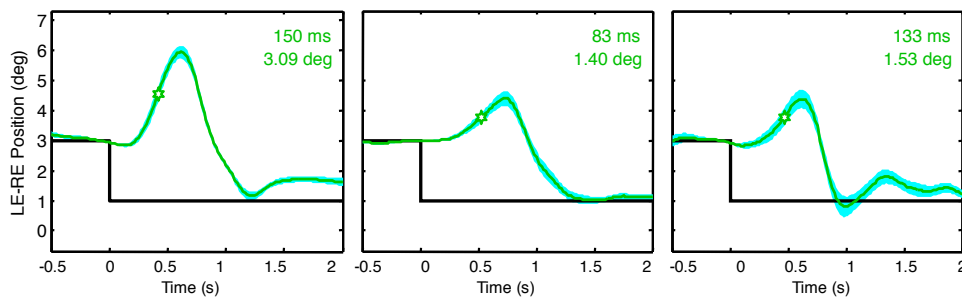


Fig. 12. Averaged convergence and divergence movements (green curves) from three individuals with anomalous compound divergence behavior (plotted with the same conventions as Fig. 3). A: examples of typical average convergence responses. B: Average divergence movements for the same three individuals. Note the low error across the repeated examples of the divergence movements, implying a non-adapting stereotypical behavior.

## Discussion

As expected, the parameters of the typical vergence dynamics were clearly distinct from those of the saccadic system. If we consider the main sequence parameters for a saccade of the size of the present vergence movements ( $1^\circ$  in each eye), it should have an expected duration of 20 ms and a velocity of 40 °/s [ i.e.,  $(200^\circ/\text{s at } 5^\circ)/5$  ] (Bahill et al., 1975a), while the typical vergence responses had the total duration of about 330 ms and a typical peak velocity in each eye of about 5 °/s for both the convergence and divergence directions (making a total vergence velocity of about 10 °/s). Thus, the vergence impetus is an order of

magnitude less efficient than the saccadic, requiring a neural drive of about 20 times longer duration.<sup>1</sup>

<sup>1</sup> We note that the extreme values of up to an average of about 70 °/s (35 °/s in each eye) for the maximum vergence velocities reported by Erkelens et al. (1989) were obtained for large vergence angles under full cue conditions. In terms of the 'main sequence' concept, these velocities were again about a factor of 20 lower than the maximum reported saccadic velocities of 600-800 °/s, and had durations of the order of a factor of 10 longer, at ~500 ms.



We may expect the total energy needed to move each eye during the vergence movement to match that of saccadic eye movements. Accordingly, Gamlin & Mays (1992) found that medial rectus motoneurons in the mid-brain had about the same integrated firing rate for saccadic and vergence movements of the same amplitude ( $4^\circ$ ). Interestingly, if we divide the saccadic velocity by the duration factor of 1/20 between saccades and vergences, this total energy hypothesis predicts a peak vergence velocity of 40/20 or  $2^\circ/\text{s}$ , which is within a factor of 2 of the measured velocity. Since these motoneurons are the final common pathway for vergence and saccadic movement control, it makes sense that they should approximately adhere to the principle of the same total energy for a given eye movement, corresponding to the same total number of motoneuron spikes, despite the order of magnitude difference in the durations of the eye movements. The factor of 2 discrepancy for vergence relative to versional movements has been validated in direct muscle force measurements by Miller, Davison & Gamlin (2011).

This analysis leaves unanswered the question of why the duration of vergence movements should be so much longer than that of saccades. Presumably, it is not evolutionarily adaptive, because the slowness of vergence movements leaves significant time for diplopia to become evident, which constitutes an undesirable failure of object coherency whenever large vergence movements are made. Instead, the slowness may derive from the physiology of the vergence control pathway, which is routed through the cerebellum rather than having a direct cortical/brainstem drive (Gamlin, 1999, 2002). Perhaps there is something in the integrative nature of cerebellar processing that requires a longer integration time than is available through the direct drive.

A key factor determining the slowness of vergence movements may well be the **inhibitory cross-coupling** via inhibitory burst neurons (Strassman et al, 1986) between the pairs of brainstem nuclei that control the ipsilateral motor neuron activation for both the lateral and medial rectus muscles (in the abducens and oculomotor nuclei, respectively). Presumably, this mechanism has evolved to inhibit the contralateral motor neurons to the corresponding muscle type in order to maximize the conjugate (parallel) pairing of the muscle activations required for saccades. Based on the relative durations of vergence and saccades, the specific proposal to account for the vergence dynamics would be that this contralateral inhibition is 90% effective or more, reducing the drive to the eye muscles for the symmetric activation of vergence movements to 10% or less of the level for the conjugate activation of saccades. As a result, the vergence system has to generate the drive for more than 10 times longer duration to achieve the same amplitude of symmetric vergence

movements as conjugate saccades, in accord with the equivalence of the time-integrated signals reported by Gamlin & Mays (1992).

### Waveform asymmetry analysis

This study introduces an index of temporal asymmetry that assesses the time-symmetry of the vergence velocity trace. This Normalized Temporal Asymmetry Index (symbolized as  $\gamma$ ) was designed to evaluate interpreting the temporal symmetry results in terms of the dual-mode model reviewed in the Introduction, consisting of an **open-loop** burst component driving disparity vergence movements and a **closed-loop** vergence tracking component corresponding to the step-response minimization of the error signal generated by the disparity step. The closed-loop response to a step change in the tonic vergence signal is expected to conform to an exponential time course (Robinson, 1975; Zee, FitzGerald & Optican, 1992), while the open-loop response should have a more symmetric form derived from an open-loop burst mechanism (Gamlin & Mays, 1992). This model generates a Normalized Temporal Asymmetry Index value of  $\gamma = 0.6 - 0.9$  for the exponential time course of closed-loop vergence eye movements. (The full asymmetry of  $\gamma = 1.0$  would correspond to a pure exponential waveform, but there is always some smoothing of the onset rise time that reduces the index below 1.0.)

The neural signals of saccadic burst neurons, on the other hand, are not exponential in form but are largely symmetrical in time in the amplitude range of most vergence movements (Becker & Fuchs, 1969; Becker, 1972; Bahill, Clark & Stark, 1975; Harris & Wolpert, 1998; 2006; Tanaka, Krakauer & Qian, 2006; Xu-Wilson et al., 2009). Thus, although in principle saccades could have the exponential form characteristic of a closed-loop continuous feedback system, in practice they approximate the time-symmetric form of a fully ballistic drive for amplitudes within the vergence range of up to about  $10^\circ$ . Since the velocity/time function of an eye movement is a reasonable proxy for the underlying motor neuron burst that drives it (Fig. 1), we may operationalize the symmetry of the velocity/time plot as an indicator of the degree of involvement of a neural burst of activation in the generation of any given eye movement. Based on the weight of the evidence, then, we will take perfect symmetry ( $\gamma = 0$ ) as implying that the eye movement is entirely driven by a neural burst, while large asymmetries of  $\gamma > 0.5$  will be assumed to imply a strong dominance by the closed-loop step response.

Based on the above analysis, the fact that the Normalized Temporal Asymmetry Index was approximately zero for the large group (62%) of typical convergence movements and for the smaller group (32%) of typical diver-

gence movements, under the present stimulation conditions of a widefield texture stimulus at a vergence amplitude of  $2^\circ$ , may be taken as suggesting that the typical vergence system response may be driven by an open-loop burst mechanism comparable to that of the saccadic system, although weaker by an order of magnitude (as indicated by the respective durations of about 400 ms vs 20 ms, respectively, for typical vergence and saccadic movements at this amplitude; cf. Figs. 3, 4 & 6). A similar result can be seen in the large vergence movements of Erkelens et al. (1989). This analysis through the Normalized Temporal Asymmetry Index thus tends to validate the dual-mode model not only for typical convergence but also for typical divergence responses (Table I). Atypical forms with high positive and even high negative symmetries are encountered in some of the groups, but in the typical range defined by durations  $< 450$  ms, the temporal asymmetry remains close to zero, similar to that of the typical convergence responses. Thus, we infer that the optimal divergence response is not fundamentally different in control dynamics from the convergence response – both are well described by the dual-mode theory of a combination of fast open-loop and more accurate closed-loop control mechanisms.

## Latencies

Before discussing the detailed properties of each of the other subgroups, a general comment on the latencies is in order. For the four groups with typical response behavior, the latencies had similar values, of 252 and 317, 275 and 283, for the pairings of convergence and divergence movements, respectively (see Table I). Similarly the mid-rate latencies, though shorter (at 198 and 200, 144 and 211 ms, respectively), failed to exceed the statistical criteria for significant differences. Thus, the atypical groups did not show any tendency to have significantly longer latencies than the typical vergence group, all being between about 150 and 320 ms, with SEMs of 25-50 ms. Similar results are evident for the Slow Divergence group. This relative invariance in the latencies gives assurance that the atypical groups were not suffering from the kinds of general neurological problems or impaired cortical decision-making capabilities that affect saccadic latencies, suggesting instead that the slowing and anomalous behavior in these cases was specific to their vergence control mechanisms once the movement was triggered.

## Slow divergence with typical convergence movements

A significant subgroup of the participants had slow divergence dynamics in conjunction with typical convergence dynamics. One subject had the reverse combination: typical divergence dynamics combined with slow convergence

dynamics. The same diversity was reported among the small group of four subjects studied by Erkelens et al. (1989), two having faster convergence and two having faster divergence for the extreme vergence movements studied there. The implication is clear, therefore, that the convergence and divergence dynamics are controlled by distinct brainstem mechanisms, either of which can show abnormalities while the other is within the normal range (in the sense that they form a large cluster with low variability of the convergence dynamics, Fig. 2). The fact that, for the majority of the participants, the convergence mechanism is within a range defined as ‘normal’ implies that it is less susceptible to neurological disruption than the divergence mechanism (whether from developmental or idiopathic etiologies). The two vergence directions both appear to be capable of similar dynamics (i.e., when both are in the typical range), but differences in dynamics in the non-typical cases suggest that they have independent control mechanisms that are differentially susceptible to prevailing forms of disruption.

The high temporal asymmetry indices for the slow divergence movements suggest that they conform to the closed-loop feedback control, (in contrast to the close-to-zero values for the typical divergence movements, implying open-loop control). Thus, the presence of two reliable forms of temporal asymmetry may be regarded as confirmation of the presence of a distinct mechanism underlying the slow disparity vergence movement behavior. The asymmetric variety may represent the operation of the closed-loop feedback mechanism in cases where the open-loop mechanism fails to operate, for either ontogenetic or adventitious post-developmental reasons.

Curiously, the convergence responses in the Slow Divergence group exhibit the unexpected behavior of a negative asymmetry, implying a gradual onset of the velocity profile rather than the gradual offset predicted by the closed-loop hypothesis. Similar behavior is seen below for the Anomalous Compound Divergence group and can be interpreted as a form of nonlinear neural recruitment, generating progressive acceleration of the movement toward the end of the response.

## Oscillatory vergence behavior as indicative of a sampled data system

Oscillatory behavior in vergence tracking tasks has been reported since Rashbass & Westheimer (1961), and has been modeled with closed-loop feedback systems driven by disparity error (Hung, 1998; Semmlow, Hung & Ciuffreda, 1986). Such closed-loop oscillations may be understood as limit cycles in the inevitable response of a delayed feedback signal, since the vergence response will reduce the error to zero, and no further vergence response will occur until a new level of disparity error is generated

(Rashbass & Westheimer, 1961). This process will repeat as long as the disparity-tracking target continues to move.

However, Rashbass & Westheimer (1961) also reported vergence oscillations in disparity vergence **step** responses in one anomalous subject (although this anomaly was dismissed by Semmlow, Hung & Ciuffreda, 1986, as a lack of fusion or noise artifact). The original authors argued that the oscillatory behavior typically seen in disparity vergence tracking tasks was most likely an indication that disparity vergence control is a sampled-data system.<sup>2</sup> The disparity step task is a specific test of this sampled-data hypothesis, which predicts **vergence oscillations** as the residual error is resampled to see how much it has been reduced toward zero as the vergence movement progresses, whereas the delayed feedback model predicts a **continuous** reduction in the vergence error as long as the residual disparity does not reach zero (and predicts oscillations only during a continuous disparity tracking task). However, this sampled-data prediction is complicated by the presence of a dual-mode vergence system, since the open-loop step response is fast enough to bring the disparity to zero within one sampling interval, implying that no oscillations would be expected in a disparity step task for normal vergence steps. Only when vergence behavior was governed by the closed-loop system would vergence oscillations be expected.

The implication of this analysis is that the anomalous subject reported by Rashbass & Westheimer (1961) could have had a weak or absent disparity-step vergence system, revealing the sampled-data mode of the closed-loop component during the extended vergence movement occurring in their step disparity task. We can test this in the present paradigm by looking at the velocity traces in cases where particular subjects had slow convergence or divergence movements (implying that their open-loop burst vergence system was weak or absent, and that they had to use the closed-loop feedback system to generate the responses to the step disparity stimulus).

Before analyzing the present data, we may consider the reported oscillatory vergence behavior by Sylvestre et al. (2002). Although these authors predict and confirm a form of oscillatory vergence behavior, they do so in the context of combined vergence and saccadic eye movements, in which vergence is very much the junior partner, with no vergence demand and amplitudes an order of magnitude smaller than the saccadic responses. Moreover, the oscillations are rapidly damped following the primary step response. This study provides only weak support for the vergence sample-data hypothesis, therefore. Finally, we note that the form of conjugate, saccadic oscillations described by Ramat et al. (2005) are not equivalent to the vergence oscillation we describe, both because the former are conjugate in the two eyes and because they are an order of magnitude faster, at around 30 Hz.

The amplitude and velocity plots for the slow responses meeting the criteria for the missing open-loop vergence system (illustrated in Fig. 10) provide a strong test of the hypothesis that the residual vergence control system is a closed-loop sampled-data feedback system. If it were a continuous feedback system (with or without delay), the slow ramp of the vergence responses and the velocity traces should be close to pure exponential functions. In fact, the velocity traces of these slow responses reveal profound oscillations in the vergence behavior, as predicted by the sampled-data hypothesis.<sup>3</sup> It seems that the vergence error is sampled only intermittently to determine whether to inject another burst of activation to further reduce the disparity error, at sampling rates of  $\sim 3$  samples/s. Bearing in mind that these are averages of 12 responses each, to asynchronous stimulus events, it seems that the sampling is typically synchronized by the stimulus event, in order that the individual responses would have averaged to a clean trace. Thus, the oscillatory form of the disparity step responses for these slow-vergence subjects implies that the closed-loop disparity vergence system is indeed a type of sampled-data system predicted by Krishnan & Stark (1977) and Hung (1998), as opposed to being

<sup>2</sup> Oscillatory responses are also characteristic of under-damped second-order control systems. However, the fact that the vergence system shares the oculomotor plant with the saccadic system, and that the saccadic waveforms of the subjects in the slow vergence oscillation group did not, in fact, exhibit any evidence of oscillations during saccades for any of the subjects with slow vergence responses (data not shown), implies that the oscillatory behavior of the slow vergence responses is more likely attributable to the alternative hypothesis of a sampled-data behavior in the neural control system for vergence than to under-damping in the oculomotor plant.

<sup>3</sup> As is evident in Fig. 10, the oscillations are a minor perturbation around the predominantly exponential waveforms in the position traces. It is only when the velocity traces are plotted that the oscillatory behavior becomes clearly visible on the basis of the relative enhancement of the higher velocities. Nevertheless, these cases are still compatible with the view that the slow responses are governed by the exponential form characteristic of closed-loop feedback control, even though the feedback derives from intermittent sampling that gives rise to the oscillatory behavior. There is insufficient data from the present sample to develop this inference quantitatively, however.

merely a delayed-feedback tracking system generating limiting cycles for the tracking behavior (although the presence of a significant feedback delay cannot be excluded by this analysis).

It should be noted that this sampled-data analysis could only be performed effectively on the small group of very slow responses, since the typical and mid-rate responses have only one or two cycles of oscillation to distinguish from the primary response, which could not be done without quantitative model fitting of the response behavior.

### Anomalous compound divergence response

In the present sample, a substantial subpopulation of about 18% of the subjects (with no strabismus on a cover test or reported history of TBI) showed an inability to make prompt divergence movements. Instead, the divergence stimulus evoked the compound response of an initial **convergence** movement comparable to the response to the convergence stimulus, followed by a larger divergence movement bringing the eyes approximately to the intended target disparity despite having initially moved in the wrong direction (Figs. 11 & 12). We have not been able to identify any previous reports of this type of oculomotor anomaly. For example, nothing of this kind is mentioned in the NEI Classification of Eye Movement and Strabismus (CEMAS) Report (2001). Even in cases of strabismus and related oculomotor disorders (Kenyon, Ciuffreda & Stark, 1980) or TBI (Thiagarajan, Ciuffreda & Ludlam, 2011), no such behavior has been reported.

It is worth considering the timing of the anomalous convergence movement in detail. Note that the anomalous initial convergence dynamics were in the typical range for convergent disparity stimuli (~300 ms in duration), and that the individual responses were usually similar for all individual trials. This result makes clear that the anomalous convergence movement in the compound movement complexes was not a saccade of some kind (which should have had a duration of only about 20 ms for this amplitude), but was a genuine convergence movement.

Why should a divergence stimulus evoke an initially convergent eye movement? Two possible explanations suggest themselves: disparity-change uncertainty and an inverse priming strategy.

1. If disparity changes were occurring unpredictably, and if the convergence and divergence subsystems were in competition with each other but with convergence slightly predominating, it might be supposed that disparity change would tend to activate the dominant response direction in **both** directions before the sign of disparity change was processed, hence activating a **convergent** response in both cases. Such a response would be appropriate for the convergence stimulus but would need correcting when the

stimulus was a **divergent** disparity. Thus, under this **disparity-change uncertainty hypothesis**, the anomalous convergence response to divergent stimuli would be a reflection of the initial uncertainty as to the direction of the disparity change. This hypothesis would also predict an appropriate direction for the convergence response, and is hence consistent with both directions of vergence behavior in these individuals.

However, although the **timing** of each stimulus event was jittered over a 1 s range in our paradigm, the **sign** (and amplitude) of each disparity change (i.e., convergent or divergent) was perfectly predictable throughout the sequence. Each convergence stimulus was followed by a divergence stimulus, and vice versa. Thus, on a cognitive level at least, the subject had every opportunity to gear up for a divergence response to each divergence stimulus. Of course, this does not necessarily imply that the directional information was available to the burst neurons generating the initial burst of activation to drive the fast onset of the divergence movement, but the system had the ~300 ms latency period before the movement took place to compute the sign of the disparity (which is about the length of the perceptual integration time for disparity processing; Tyler & Julesz, 1980; Tyler, 1983), so there is little reason to suppose that the disparity information would not have been available. The disparity-change uncertainty explanation thus seems relatively implausible.

2. The other hypothesis to account for these anomalous compound divergence movements is an 'inverse priming' strategy for divergence initiation. This hypothesis is based on the concept that there is some impediment to initiating a divergence movement, and that making a convergence movement primes the system to a state of readiness to be able to implement the required divergence movement. This priming mechanism could be similar to the priming of secondary express saccades (Fischer & Ramsperger, 1984; Takagi, Frohman & Zee, 1985; Fischer, Weber & Biscaldi, 1993; Coubard, Daunys & Kapoula, 2004; Van Koningsbruggen & Rafal, 2009). On this hypothesis, these anomalous compound divergence movements are manifesting some deficiency in the divergence system that derives in the ability to **initiate** divergence movements. Making the anomalous convergence movement would release the system from this initiation defect and allow the divergence mechanism to operate normally from that point onwards.

It should be stressed that the variability of the compound divergence movements was of the order of 0.1° or less, implying that the vergence behavior was highly consistent across the 12 stimulus repeats despite the recurring knowledge that the initial movement was incorrect each time. Thus, on balance the repeatability of the anomalous compound behavior seems to favor the inverse priming



hypothesis, but the idea that the disparity sign signal is not reaching the brainstem control nuclei in these individuals cannot be excluded.

Once primed, the divergence movement typically has sufficient amplitude to overcome the convergence error, and to reach the appropriate divergence angle for the target. However, the temporal asymmetries for these compound divergence movements were large, close to the exponential prediction, implying that the divergence systems the open-loop burst mechanism in these individuals was lacking or weak. The convergence responses in this group, however, had the opposite character with a strong **negative** asymmetry, implying gradual build up of the velocity with a more rapid response offset. This form of asymmetry is consistent with a progressive recruitment of activation following the response onset, perhaps by positive feedback (as opposed to the progressive decay of the activation implied by negative feedback.)

### Saccades and vergence/saccadic interactions

The saccade measures of Fig. 6 are included to emphasize the profound difference in time scale between vergence and saccadic step responses. Although it was not the main topic of this paper, we note in passing that the 20° saccades analyzed for the ‘typical’ subpopulation had a highly stereotypical behavior, with each subject showing some stable degree of undershoot of the initial saccade, followed by a stereotypical corrective saccade to reach the repetitively presented target (Fig. 6). Despite performing 24 back-and-forth movements between the same two targets, there was no tendency to correct the initial saccadic amplitude to reach the target in one shot. This result is consistent with the initial reports of corrective saccades (Becker & Fuchs, 1969; Becker, 1972), and may reflect the tendency to perform combined eye and head movements for large changes in stimulus position, even though head movements were eliminated by our chin and forehead restraints.

With respect to saccadic/vergence interactions, we found no evidence of a consistent saccadic component in the averaged vergence responses (see Fig. 7). Although there were often refixations within the range of the 1.25° fixation target, they did not occur at a systematic timing relative to the vergence onset, and therefore could not be analyzed in a consistent fashion. The symmetric disparity vergence behavior for the present population is best characterized as being fully controlled by the vergence system with no significant interaction with the saccadic system.

## Conclusion

This survey of vergence dynamics in non-academic population sample showed a remarkable variety of vergence behaviors. The population was subdivided into nine main groups according to whether the convergence/divergence dynamics were typical, moderately slowed or severely slowed: typical vergence dynamics, atypically slow dynamics of either convergence and divergence or both, moderately slowed dynamics of either convergence and divergence (with severe slowing of the other) or both, anomalous compound divergence behavior, and mixed or inconsistent vergence responses.

The results could be interpreted in terms of the dual-mode analysis of vergence responses consisting of a combination of an open-loop burst response and a closed-loop feedback response in each vergence direction. The vergence dynamics for disparity jumps of a large textured field have a typical time course consistent with predominant control by the open-loop vergence-specific burst mechanism, although the subgroups showed radically different vergence behaviors. Some subjects showed markedly slow divergence responses, implying that the two vergence directions have separate control mechanisms, most likely each with separate open-loop burst and closed-loop feedback subsystems (though cases of slow convergence are rare). A further type of behavior in a distinct subgroup was a compound divergence response consisting of an initial convergence movement followed by a large corrective divergence movement, in which both have normal time courses implying open-loop burst control.

The cases of slow responses to disparity steps exhibited pronounced oscillations in the velocity trace at about 3 Hz, implying that these cases were governed by a sampled-data system at a rate of about 3 samples/s. Thus, the variety of human vergence dynamics contributes substantially to the understanding of the oculomotor control mechanisms underlying the generation of these movements.

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## Figure Captions

Fig. 1. Monkey vergence response reproduced from Gamlin & Mays (1992), showing the right and left horizontal eye position traces (HR, HL), the difference trace of vergence amplitude (VA), the corresponding vergence velocity trace (HLV) and the concomitant change in firing rate of a midbrain medial rectus motor neuron recorded in the oculomotor nucleus during the movement. Note the similarity between the waveform of the velocity trace and motor neuron firing burst, which both have relatively long durations of about 200 ms.

Fig. 2. Top panel: Gaussian Mixture Model cluster analysis of all well-formed vergence response durations, showing the fit for the optimal 3-Gaussian case (red, green and blue curves), with respective mean  $\pm \sigma$  parameters. Center panel: Distribution of convergence duration clusters with cluster boundaries at 451 and 945 ms. Bottom panel: Distribution of divergence duration clusters, similarly.

Fig. 3. Upper plots: Examples of typical mean convergence responses for three individuals (green curves, each averaged over 10-12 responses). Black line indicates the stimulus disparity change event. Gray dotted lines show the estimated amplitude and duration of each vergence movements. Cyan region represents the  $\pm 1$  SEM range of the variability over the 10-12 repeats for each trace. The star marks the point of peak velocity. Lower plots: Corresponding velocity profiles for the same average responses (color curve), together with the time-inverted velocity profile (light gray curve) aligned with the peak of each response to illustrate its degree of temporal asymmetry, quantified above each velocity panel. Note the high degree of symmetry (near-zero asymmetry) of these typical examples. Duration and peak velocity values are estimated from the velocity trace as described in Methods.

Fig. 4. Examples of typical mean divergence responses and velocity traces for the same sample of typical subjects and plotted with the same conventions as Fig. 3. Note the high degree of symmetry (near-zero asymmetry) of these typical examples of divergence.

Fig. 5. Examples of typical mean vergence responses and velocity traces for responses showing temporal asymmetries, plotted with the same conventions as Fig. 3. A: Convergence/divergence example from the Mid Both category. B: Convergence/divergence example from the Slow Divergence Only category. C: Divergence example from the Anomalous Compound Divergence category, analyzing the **same divergence response** for asymmetry separately in the two vergence directions.

Fig. 6. Average position and velocity traces for leftward (upper panels) and rightward (lower panels) saccades averaged over 12 repeats for the subjects of Figs. 3 and 4, showing the similar latencies and much faster time courses in relation to the vergence responses. The SEM as a function of time is shown as the pink shaded region around the traces. The fact that this error region is barely visible reveals the high consistency of the saccadic performance, including the corrective saccade following the main saccade in most cases.

Fig. 7. Example of the saccades occurring during a vergence stimulation series of 1-3° vergence jumps over 12 irregular cycles (black line). The vergence signal of the difference in position between the two eyes (green curve) shows an approximate match to the stimulus disparity with a delay of a few hundred milliseconds. The mean position of the two eyes over time (magenta curve) shows general stability around the mean stimulus position (zero disparity) overlaid with microsaccades of less than 1° amplitude, which often occur at or after the completion of the vergence responses.

Fig. 8. Examples of typical mid-rate convergence responses and velocity traces plotted with the same conventions as Fig. 3.

Fig. 9. Examples of vergence movements from three individuals with typical convergence responses but slow divergence movements, plotted with the same conventions as Fig. 3. The vergence movements are repeatable to within a standard error of a few arc min.

Fig. 10. Assemblage of the mean vergence amplitude (upper plots) and velocity (lower plots) waveforms for a sample of vergence responses meeting the criteria of a duration > 1 and an asymmetry index > 0.5. Note pronounced oscillations in the vergence velocity plots (colored curves). Other conventions as in Fig. 3.

Fig. 11. An individual 60 s time series of step disparity vergence movements in one case, showing repeated anomalous compound responses to the divergent disparity stimulus, with the divergence movement preceded consistently by a full convergent movement in the opposing direction. Black trace is the stimulus disparity to be tracked. Note that none of these anomalous vergence movements had a significant contribution from differential (asymmetrical) saccades, which appear as fast spikes on this time scale. The saccades on cycles 3, 7 and 10 are all bidirectional, with little net effect on the vergence angle.

Fig. 12. Averaged convergence and divergence movements (green curves) from three individuals with anomalous compound divergence behavior (plotted with the same conventions as Fig. 3). A: examples of typical average convergence responses. B: Average divergence movements for the same three individuals. Note the low error across the repeated examples of the divergence movements, implying a non-adapting stereotypical behavior.